

CITY SCHOOL OF EDUCATIONAL INSTITUTE, PANDHURNA

OPEN BOOK EXAMINATION 2020-21

Class-10th

Subject- Mathematics

Time – 3 hour

Max. Mark– 100

General Instructions:-

1. All questions are compulsory.

2 Section A is Q.1 to Q.5 are objective type questions. Solve as directed.

Internal choices are given.

3. Section B is from Q.6 to Q.11, each carries 3 marks.

4. Section C is from Q.12 to Q.16, each carries 4marks.

5. Section D is from Q.17 to Q.21, each carries 5 marks.

5. Section E is from Q.22 to Q.23, each carries 6 marks

Section-A

Q.1- Choose the correct option and write-

i) n^2-1 is divisible by 8, if n is-

a)integer b)natural number c)odd integer d)even integer

ii)The degree of polynomial in quadratic polynomial will be-

a)1 b)2 c)3 d)Infinity

iii)If $\frac{1}{2}$ is a root of equation $x^2+kx-5/4=0$, then the value of k is-

a) 2 b)-2 c)1/4 d)1/2

iv)30th term of AP : 10,7,4,.....is:

a)97 b)77 c)-77 d)-87

v)11th term of the AP:-3,-1/2,2,.....is:

a)28 b)22 c)-38 d)48

Q.2-Fill in the blanks-

(i) All circles are _____. (congruent, similar)

(ii) All squares are _____. (similar, congruent)

(iii) All _____ triangles are similar. (isosceles, equilateral)

(iv) Two polygons of the same number of sides are similar, if (a) their corresponding angles are _____ and (b) their corresponding sides are _____. (equal, proportional)

Q.3-Match the column –

Column A

- Lines are coincident
- Lines are intersecting
- Lines are parallel
- Line intersects x-axis
- Line intersects y-axis

Column B

- y= 0
- x=0
- Infinitely many solutions
- A unique solution
- No Solution

Q.4-Write True/False-

- i. The graph of a quadratic equation is a straight line.
- ii. Each natural number is a whole number.
- iii. A polynomial of degree 3 is quadratic polynomial.
- iv. A quadratic equation has many solutions.
- v. The terms of an AP are always in ascending order.

Q.5-Answer in one word/Sentence-

- I. What is the least number that must be added to 1056 so the number is divisible by 23?
- II. Solve the following pair of equations: $2x+y=7$ and $3x+2y=12$?
- III. If $\sec\theta + \tan\theta = x$, then $\tan\theta$ is :
- IV. What will be the reflection of the point (4, 5) about the X-axis, in the fourth quadrant?
- V. If the third and the ninth terms of an AP are 4 and -8 respectively, which term of this AP is zero?

Section-B

Q.6- Show that any positive odd integer is of the form $6q+1$, or $6q+3$, or $6q+5$, where q is some integer.

Q.7. Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

- (i) $x^2 - 2x - 8$
- (ii) $4s^2 - 4s + 1$
- (iii) $6x^2 - 3 - 7x$

Q.8. In $\triangle ABC$ right angled at B, $AB = 24$ cm, $BC = 7$ m. Determine

- (i) $\sin A$, $\cos A$
- (ii) $\sin C$, $\cos C$

Q.9. Find the distance between the following pairs of points:

- (i) (2, 3), (4, 1) (ii) (-5, 7), (-1, 3) (iii) (a, b), (- a, - b)

Q.10. Write first four terms of the A.P. when the first term a and the common difference are given as follows

- (i) $a = 10$, $d = 10$
- (ii) $a = - 2$, $d = 0$

(iii) $a = 4, d = -3$

Q.11. Aftab tells his daughter, "Seven years ago, I was seven times as old as you were then. Also, three years from now, I shall be three times as old as you will be." (Isn't this interesting?) Represent this situation algebraically and graphically.

Section-C

Q.12. Use Euclid's division lemma to show that the square of any positive integer is either of form $3m$ or $3m + 1$ for some integer m .

Q.13. Divide the polynomial $p(x)$ by the polynomial $g(x)$ and find the quotient and remainder in each of the following :

(i) $p(x) = x^3 - 3x^2 + 5x - 3, g(x) = x^2 - 2$

(ii) $p(x) = x^4 - 3x^2 + 4x + 5, g(x) = x^2 + 1 - x$

(iii) $p(x) = x^4 - 5x + 6, g(x) = 2 - x^2$

Q.14. Prove that $3 + 2 \cdot 5^{1/2}$ is irrational.

Q.15. If $\sin A = 3/4$, calculate $\cos A$ and $\tan A$.

Q.16. Name the type of quadrilateral formed, if any, by the following points, and give reasons for your answer:

(i) $(-1, -2), (1, 0), (-1, 2), (-3, 0)$

(ii) $(-3, 5), (3, 1), (0, 3), (-1, -4)$

(iii) $(4, 5), (7, 6), (4, 3), (1, 2)$

Section-D

Q.17. E and F are points on the sides PQ and PR respectively of a ΔPQR . For each of the following cases, state whether $EF \parallel QR$.

(i) $PE = 3.9 \text{ cm}, EQ = 3 \text{ cm}, PF = 3.6 \text{ cm}$ and $FR = 2.4 \text{ cm}$

(ii) $PE = 4 \text{ cm}, QE = 4.5 \text{ cm}, PF = 8 \text{ cm}$ and $RF = 9 \text{ cm}$

(iii) $PQ = 1.28 \text{ cm}, PR = 2.56 \text{ cm}, PE = 0.18 \text{ cm}$ and $PF = 0.63 \text{ cm}$

Q.18. For the following A.P.s, write the first term and the common difference.

(i) $3, 1, -1, -3 \dots$

(ii) $-5, -1, 3, 7 \dots$

(iii) $1/3, 5/3, 9/3, 13/3 \dots$

(iv) 0.6, 1.7, 2.8, 3.9 ...

Q.19. (i) John and Jivanti together have 45 marbles. Both of them lost 5 marbles each, and the product of the number of marbles they now have is 124. Find out how many marbles they had to start with.

(ii) A cottage industry produces a certain number of toys in a day. The cost of production of each toy (in rupees) was found to be 55 minus the number of toys produced in a day. On a particular day, the total cost of production was Rs 750. Find out the number of toys produced on that day.

Q.20. The cost of 2 kg of apples and 1 kg of grapes on a day was found to be Rs 160. After a month, the cost of 4kg of apples and 2 kg of grapes is Rs 300. Represent the situation algebraically and geometrically.

Q.21. Give examples of polynomial $p(x)$, $g(x)$, $q(x)$ and $r(x)$, which satisfy the division algorithm and

(i) $\deg p(x) = \deg q(x)$

(ii) $\deg q(x) = \deg r(x)$

(iii) $\deg r(x) = 0$

Section-E

Q.22. State whether the following are true or false. Justify your answer.

(i) The value of $\tan A$ is always less than 1.

(ii) $\sec A =$ for some value of angle A .

(iii) $\cos A$ is the abbreviation used for the cosecant of angle A .

(iv) $\cot A$ is the product of \cot and A

(v) $\sin \theta =$, for some angle θ

Q.23. Let $A(4, 2)$, $B(6, 5)$ and $C(1, 4)$ be the vertices of ΔABC .

(i) The median from A meets BC at D . Find the coordinates of point D .

(ii) Find the coordinates of the point P on AD such that $AP: PD = 2:1$

(iii) Find the coordinates of point Q and R on medians BE and CF respectively such that $BQ: QE = 2:1$ and $CR: RF = 2:1$.

(iv) What do you observe?

(v) If $A(x_1, y_1)$, $B(x_2, y_2)$, and $C(x_3, y_3)$ are the vertices of ΔABC , find the coordinates of the centroid of the triangle